

*Complexions for Informed Design*

# **CHARACTERIZATION AND MODELING OF COMPLEXION ENGINEERED MICROSTRUCTURES**

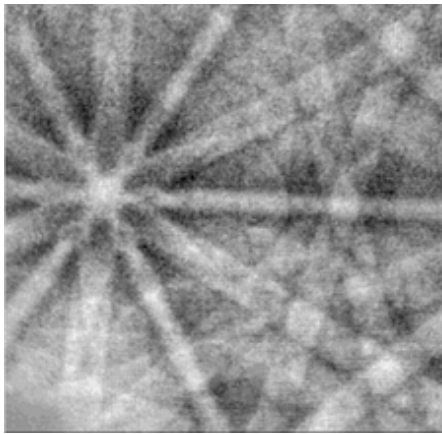
GREG ROHRER AND TONY ROLLETT

# Outline

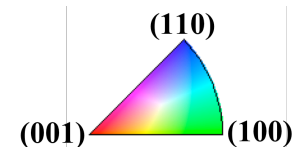
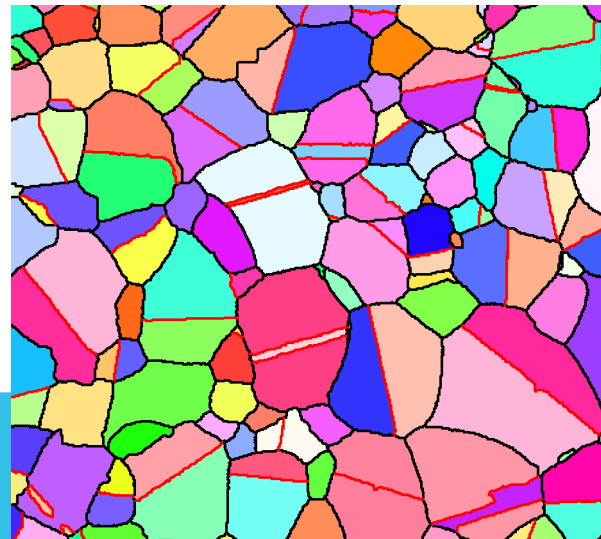
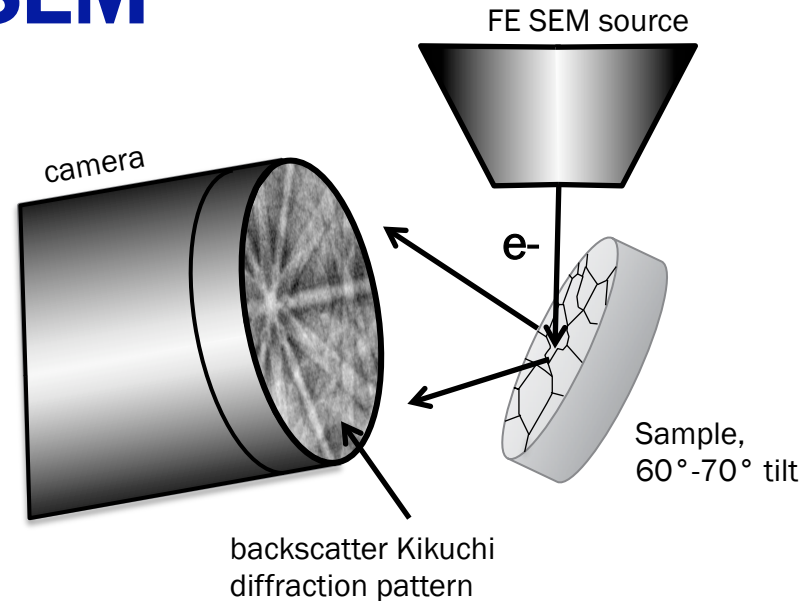
**1. Mesoscale characterization and Modeling of complex engineered microstructures**

2. Characterizing and modeling Interface distributions in nanoscale materials

# All Measurements Based on Orientation Mapping in the SEM



Electron backscattered diffraction pattern, indexed by computer

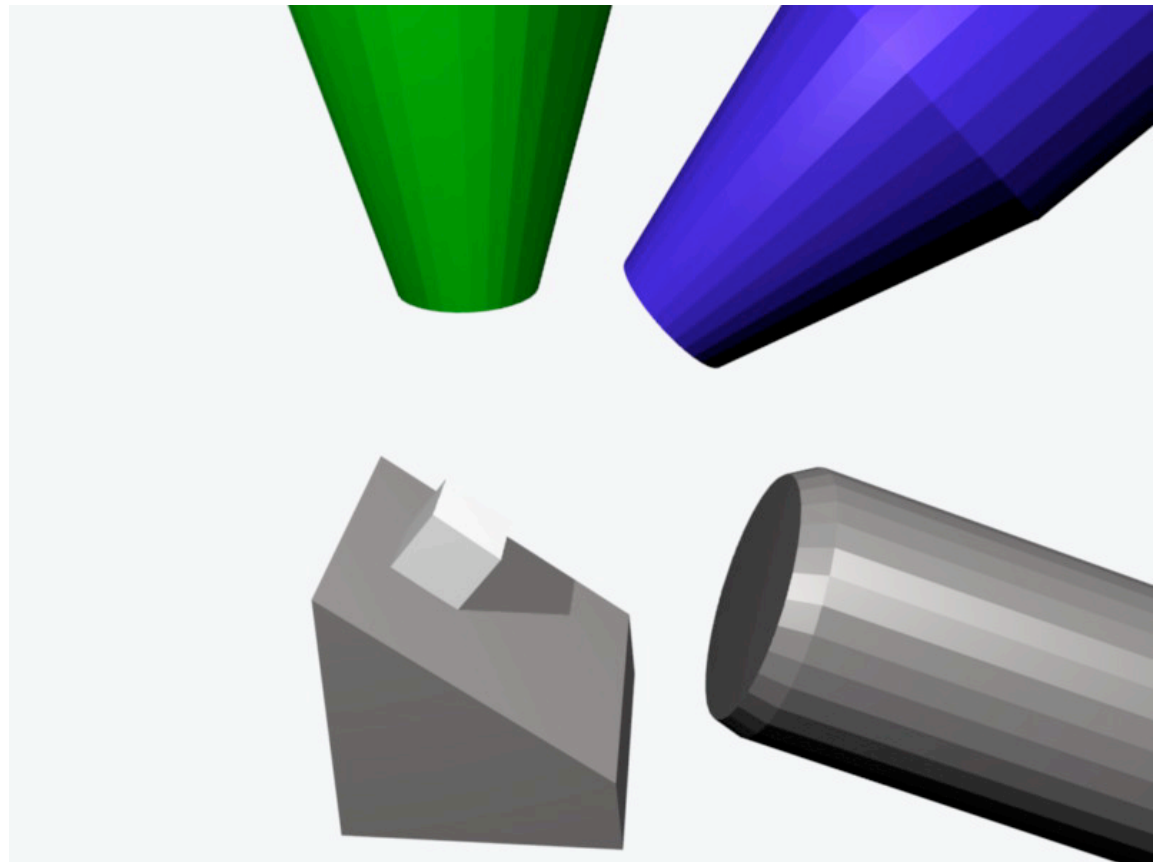
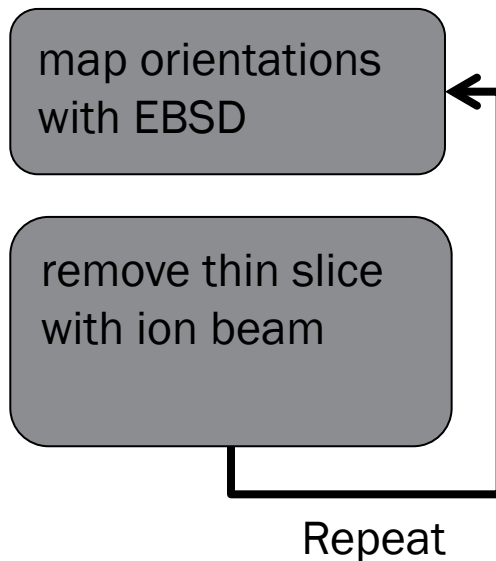


Inverse pole figure map (TiO<sub>2</sub>) displays accumulated orientations.

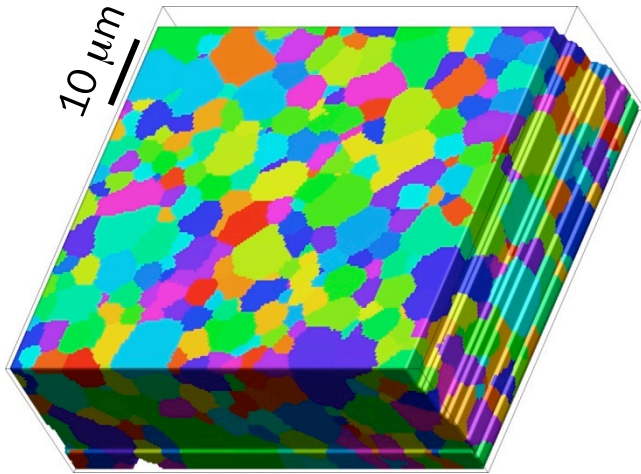
100μm

# Automated Serial Sectioning in the FIB

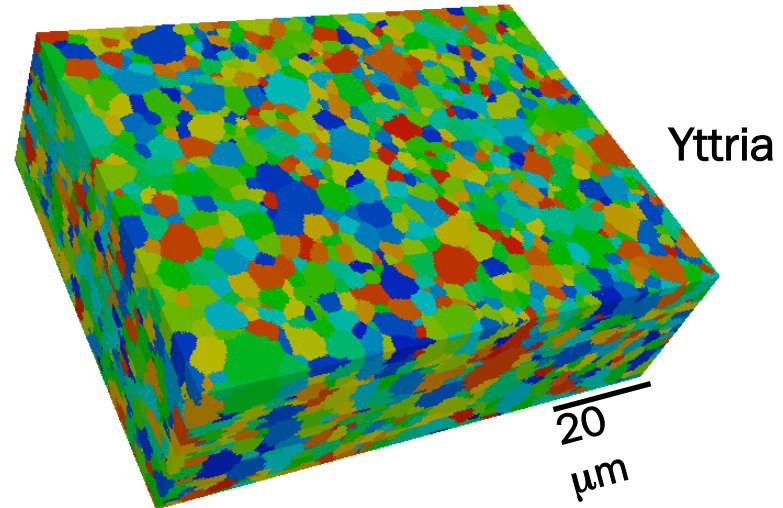
Nova 600 NovaLab  
DB-FIB SEM



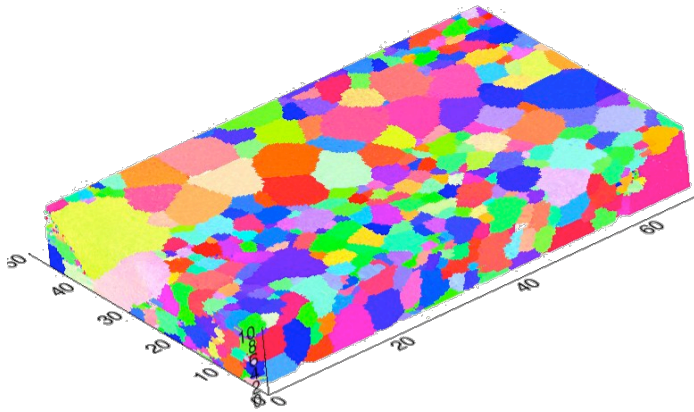
# Some of the Materials Studied



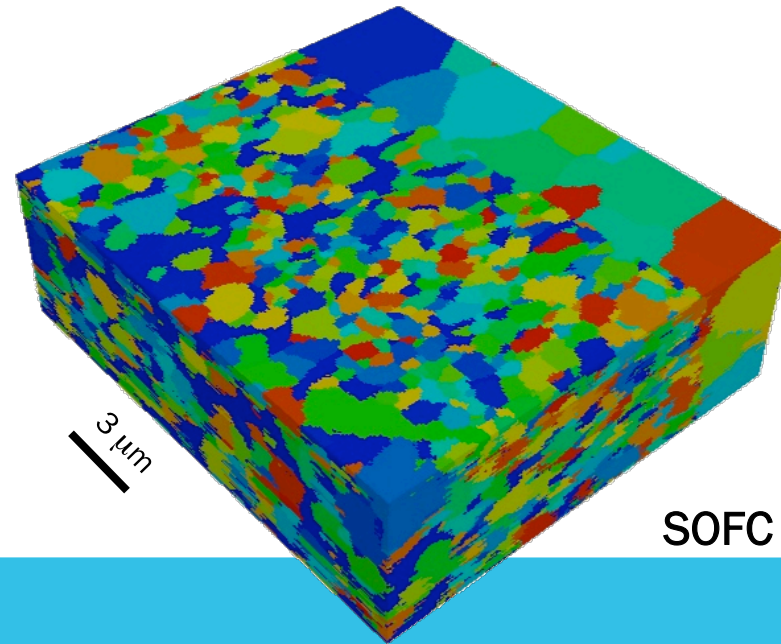
Yttria-Stabilized Zirconia



Yttria



Strontium Titanate

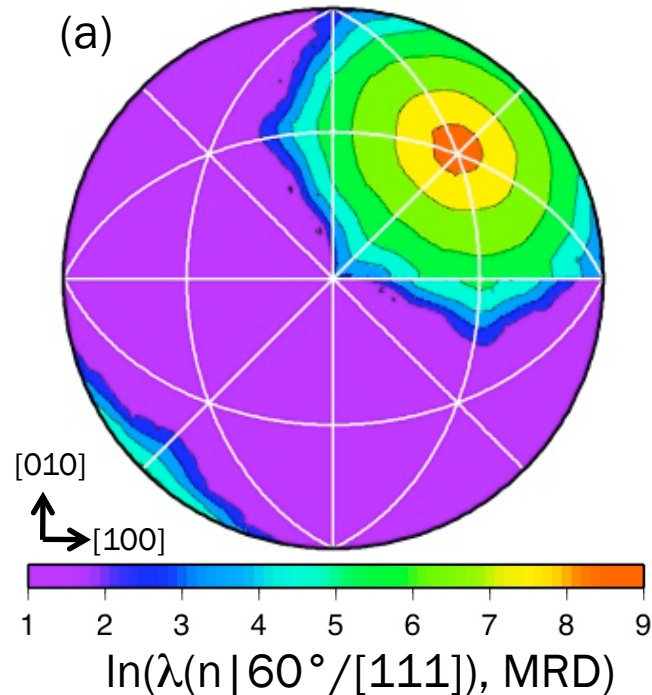


SOFC

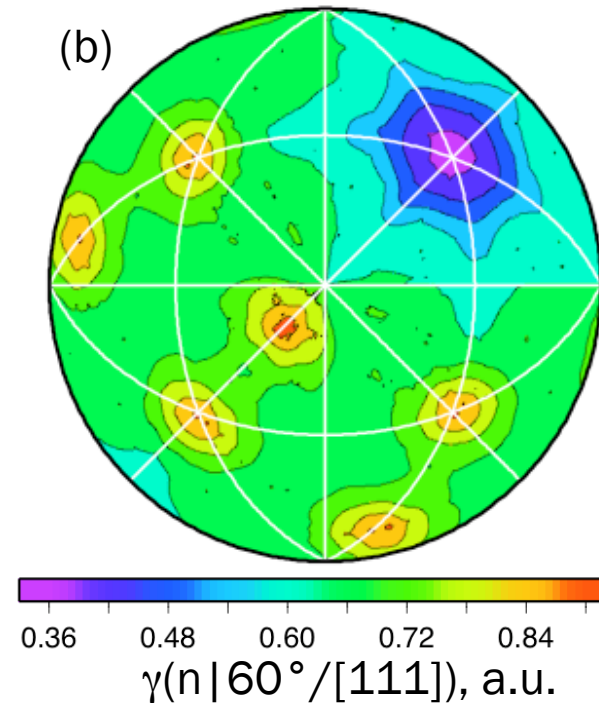
# Distribution of GB planes and energies in the bicrystal reference frame - Ni

## $\Sigma 3$ – Grain Boundary

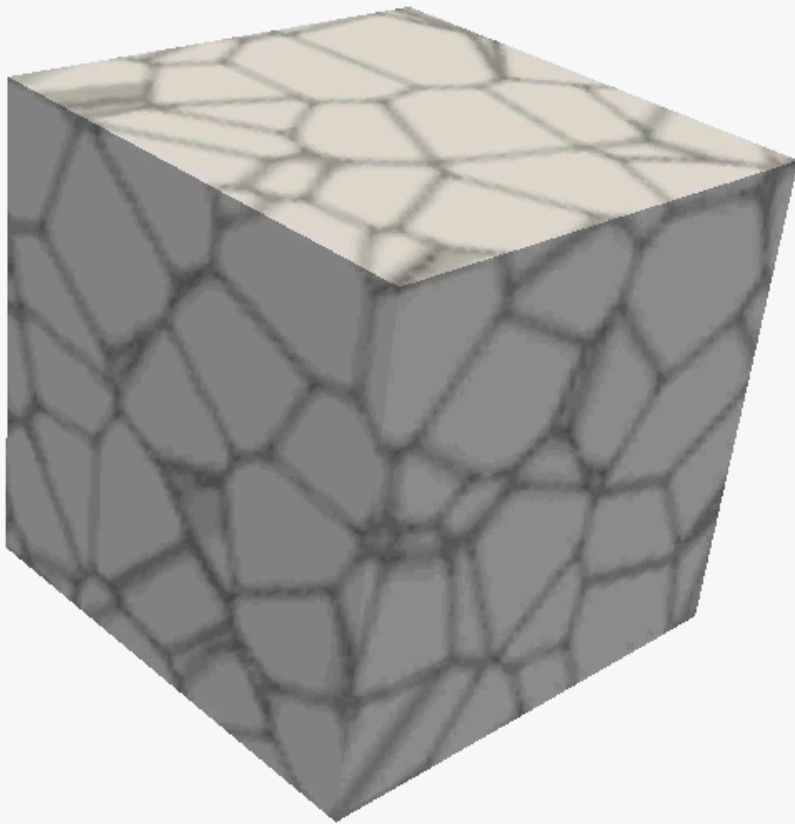
Grain Boundary Plane Distribution



Grain Boundary Energy Distribution



# Accurate simulations of microstructure evolution

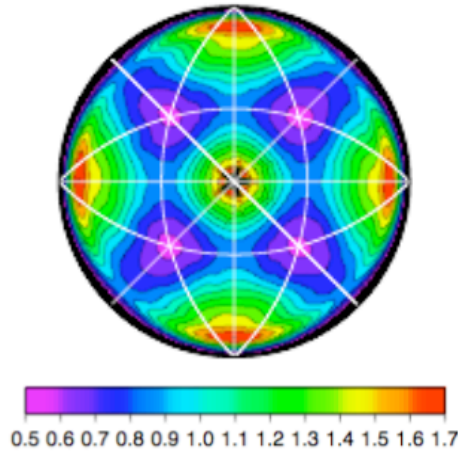


- Test models for transition from normal to complexion state.
  - Detailed modeling of solute-boundary interaction for isolated grains, and polycrystal networks.
  - Models use information about solute-GB interaction from atomistic scale simulations & theory.
- Test ideas about how mixtures of normal and complexion state boundaries influence grain growth.
  - Larger scale models with constitutive descriptions of normal $\leftrightarrow$ complexion transitions based on atomistic and detailed mesoscale modeling

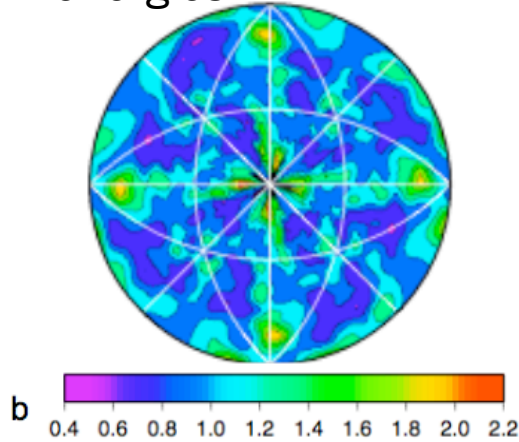


# Results of Simulations of Ni

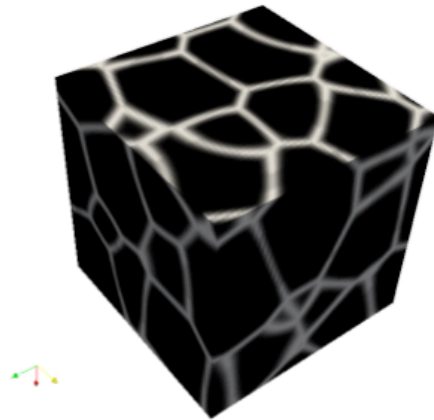
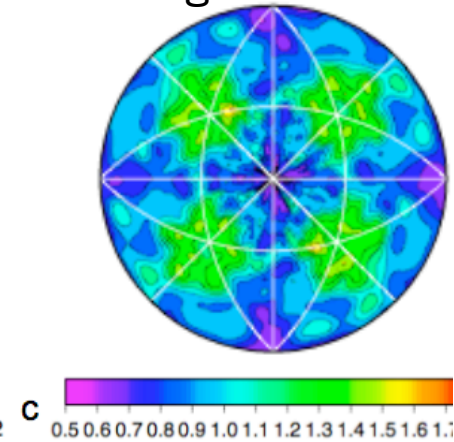
Assumed Energy  
Distribution



Interface distribution  
assuming isotropic  
energies

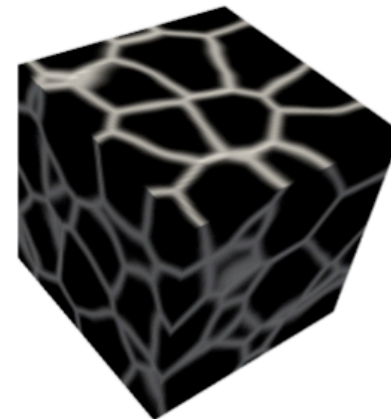


Interface distribution  
assuming anisotropic  
energies



Note differences in  
dihedral angles

e





# Systems To Study in MURI

## Initial work:

Ni-Bi (this will connect with ongoing research at Lehigh and Clemson)

## Next Priority:

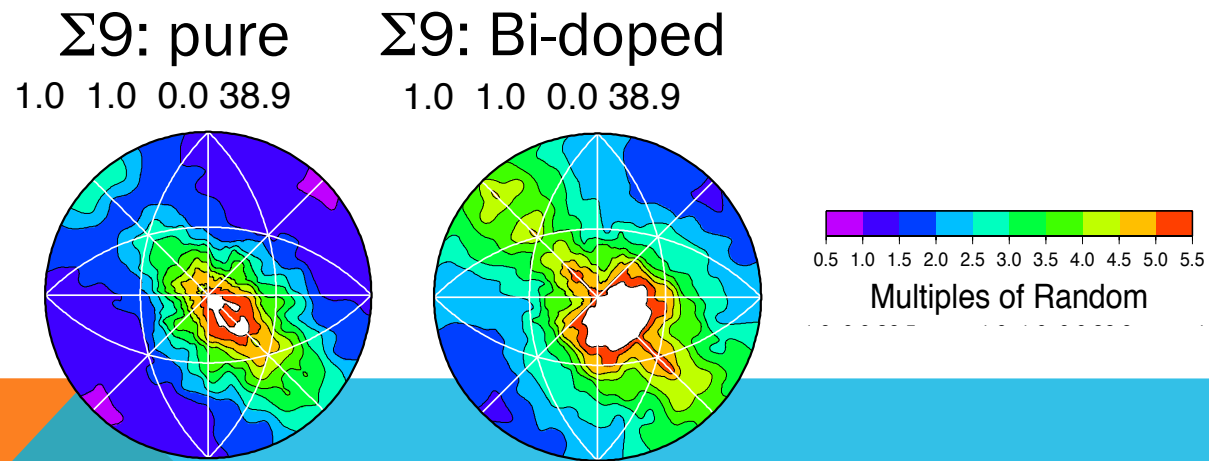
Metal Complexionized Ceramics (This will start after successful synthesis by Lehigh)

## Exploratory systems:

WC-Co (Model metal-ceramic system that has evidence of complexions)

Sn and Sb-doped ZnO (exploratory system that has evidence for complexions)

YSZ (collaborating with the Clemson and Illinois groups)



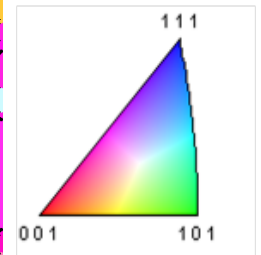
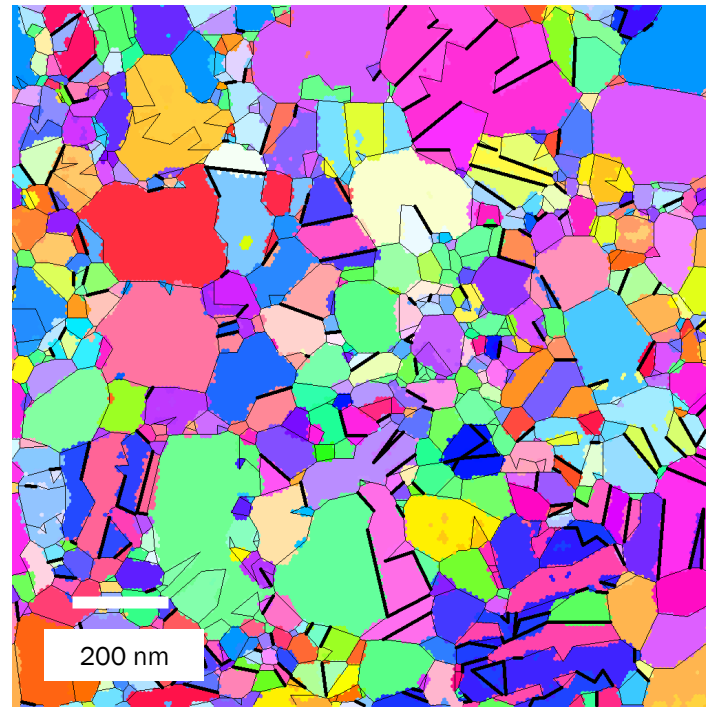
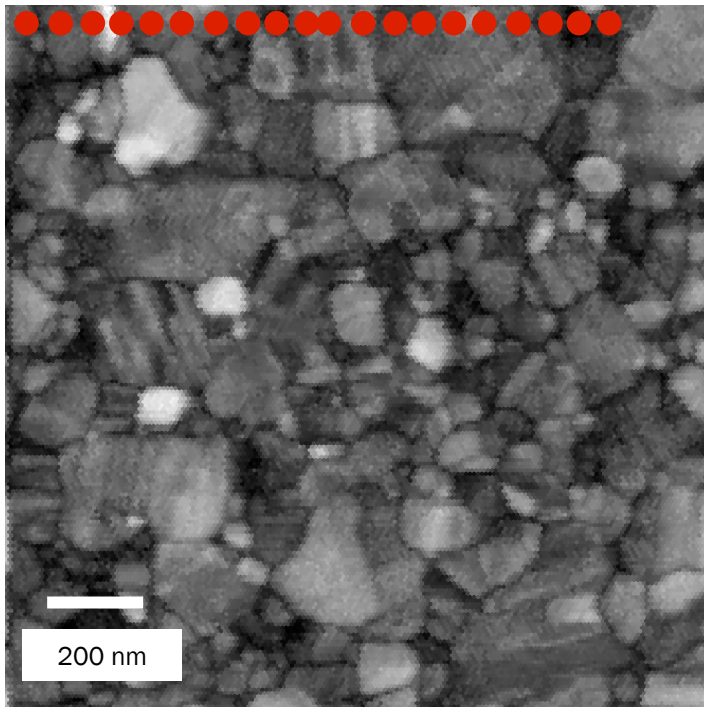
# Outline

1. Mesoscale characterization and Modeling of complex engineered microstructures

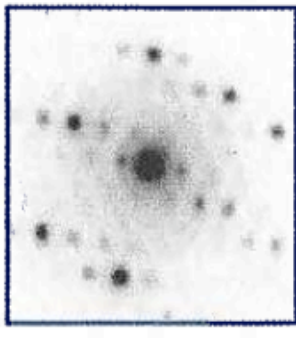
2. Characterizing and modeling Interface distributions in nanoscale materials

# Orientation Mapping at the Nanoscale

Accurate orientation mapping of a Cu thin Film with a mean grain size of 86 nm!



Inverse pole figure map with reconstructed boundaries.

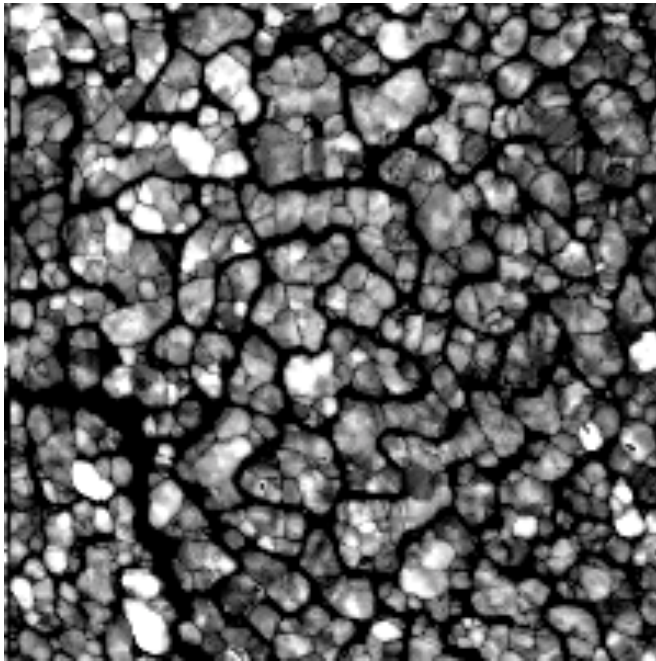


NanoMegas has developed a commercial package known as **ASTAR** that combines nanoprobe with precession diffraction.

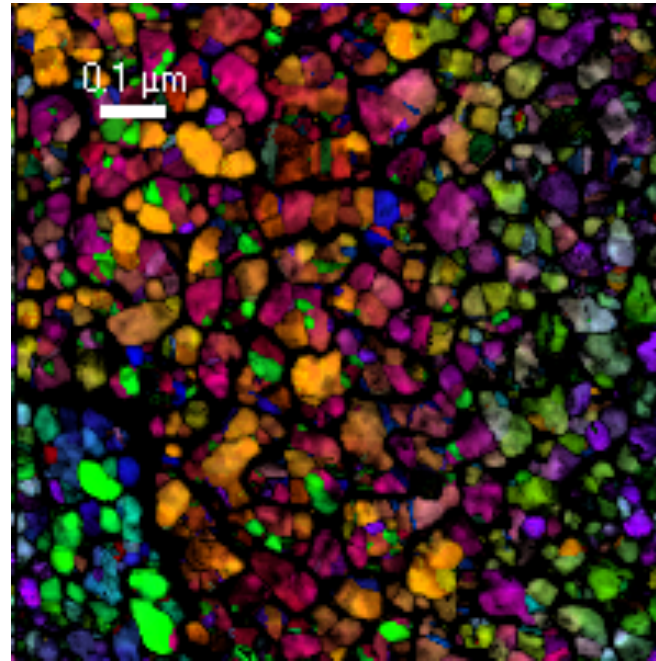
Courtesy of: A. Darbal and K. Barmak

# Orientation Mapping at the Nanoscale

Confidence Map



Orientation Map



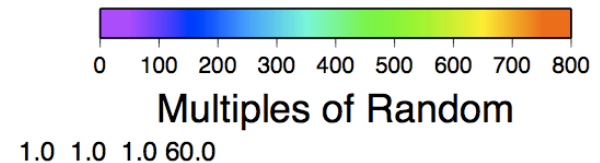
Fe:Pt thin film hard disc drive material

Courtesy of: S. Granz, M. Kryder

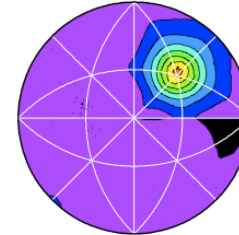
# Nanoscale Interface Data

- Compute Interface distributions
- Compute grain boundary energies
- Use as input for Phase Field Models

$\Sigma 3$  boundaries in a thin Cu film



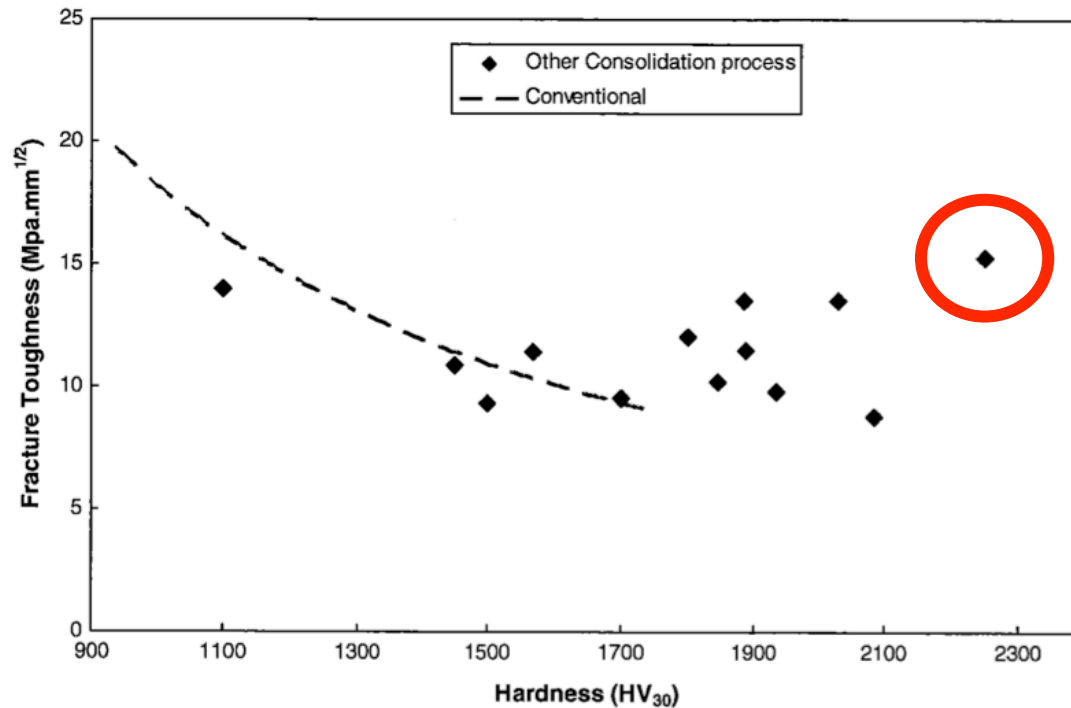
1.0 1.0 1.0 60.0



Computed based data from  
Darbal and Barmak

# Systems of interest

## Nanosized WC/Co



- Extend to other systems produced by SPS

$\text{Y}_2\text{O}_3$ -doped aluminas

$\text{SiO}_2$ -doped aluminas

Metal complexionized ceramics

Z. Z. Fang, X. Wang, T. Ryu, K. S. Hwang, and H. Y. Sohn, "Synthesis, sintering, and mechanical properties of nanocrystalline cemented tungsten carbide - a review," *International Journal of Refractory Metals & Hard Materials*, **27** [2] 288-99 (2009).



# Summary

## 1. Characterization and Modeling of complexion engineered microstructures

### - Techniques

3D mesoscale interface structure studies (GBCD measurements)

Grain Boundary Energy Measurements (towards complexion selection rules)

Modeling Microstructure evolution (phase field method)

### - Systems (possible)

Ni-Bi, Metal Complexionized Ceramics, WC-Co, ZnO-Sn,Sb, YSZ

## 2. Characterizing Interface Distributions in nanoscale materials

### - Techniques

Use emerging TEM-based orientation mapping (nanomegas system)

3D structural studies of the GB CD and GB ED

Modeling Microstructure evolution (phase field method)

### - Systems

WC-Co, Ytria and silica doped aluminas

## 3. Work accomplished by two MSE graduate students integrating characterization and modeling.

Extras



# PHASE FIELD MODEL

## FORMULATION

$$\{\phi\} = \{\phi_1, \phi_2, \dots, \phi_N\}$$

$$F(\{\phi\}) = \int_{\Omega} (f^{pot}(\phi) + f^{kin}(\phi)) dV$$

$$\sum_{i=1}^N \phi_i(x, t) = 1$$

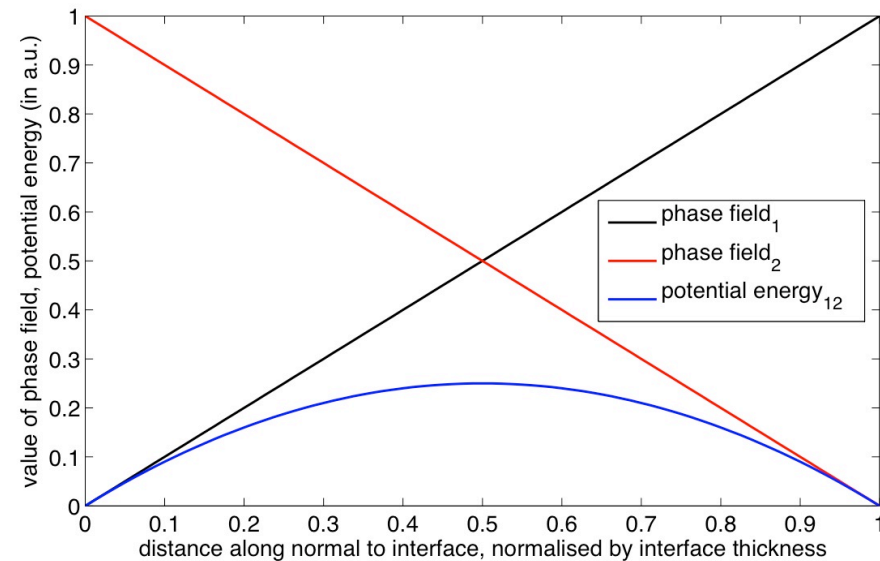
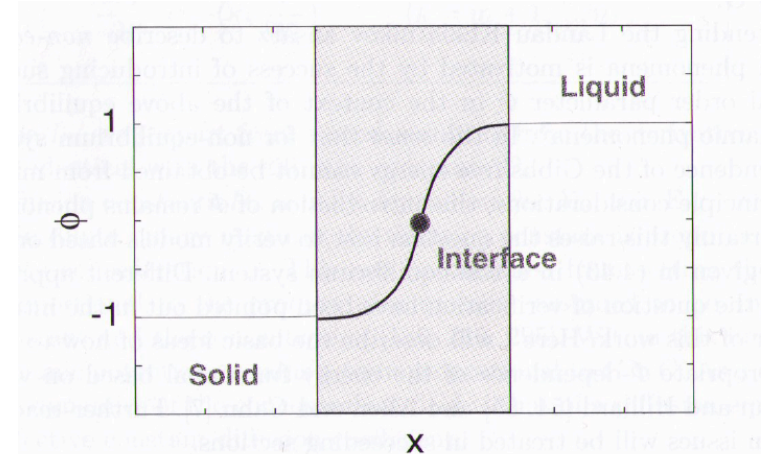
For grain  $i$ ,

$$\phi_k = \delta_{ik}, 1 \leq k \leq N$$

$f^{pot}(\phi)$  defined such that it is at a minima within each grain interior

$$f^{pot} = \sum_{\alpha=1}^N \sum_{\beta=\alpha+1}^N w_{\alpha\beta} |\phi_{\alpha}| |\phi_{\beta}|$$

$$f^{kin} = \sum_{\alpha=1}^N \sum_{\beta=\alpha+1}^N \frac{\epsilon_{\alpha\beta}}{2} \nabla \phi_{\alpha} \nabla \phi_{\beta}$$



Steinbach, *Physica D* 134 (1999) 385–393.

*Diffuse interface approach in materials science*, ed. Emmerich, p40

# SOLUTE DRAG

*What is the equilibrium segregation  $C_B^{eq}$  as a function of boundary velocity?*

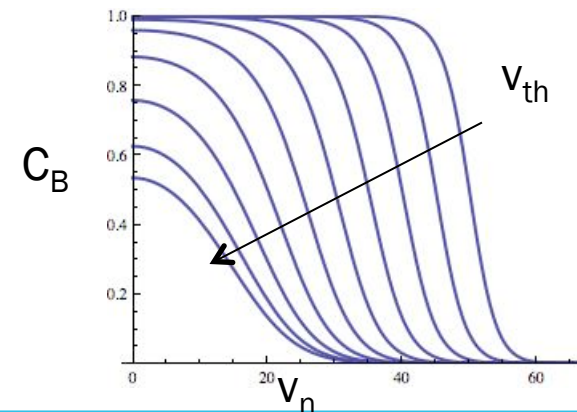
$$\mathbf{j}^{\pm} = \pm C_V^{\pm} \mu K (C_B - C_B^{eq}) \mathbf{n}$$

Approximate the  
boundary as a two-state  
system

	Energy
Bound state	$-E_0 + mv_n^2/2$
Unbound state	$mv_{th}^2/2$

The canonical distribution from  
statistical mechanics then implies

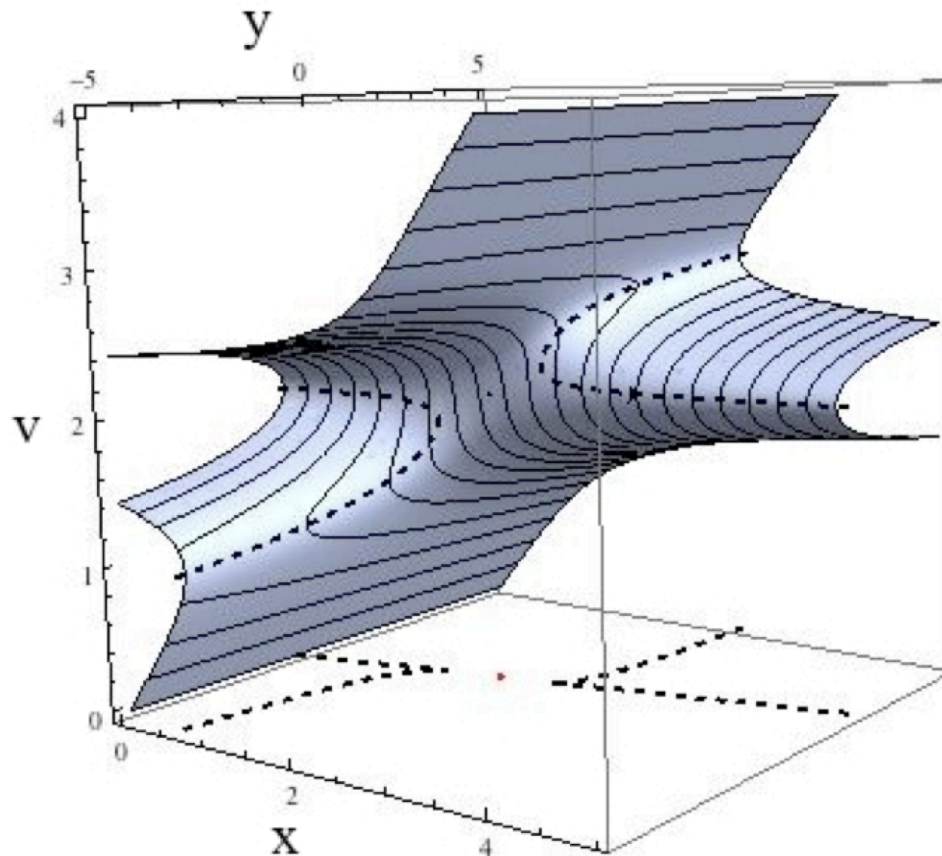
$$\Gamma_2^{eq} = (\Gamma - \Delta\Gamma) \frac{e^{-\beta\epsilon_2}}{e^{-\beta\epsilon_1} + e^{-\beta\epsilon_2}}$$



# SOLUTE DRAG

Rate of change of  
boundary velocity,  $v$ ,  
with respect to driving  
force,  $\tau$ .

$$\frac{\partial v}{\partial \tau} = -v - yv \operatorname{sech}^2 [\delta + \omega (1 - v^2)] + x$$



$$\frac{\partial v_n}{\partial t} = -L \frac{\delta}{\delta v_n} \frac{dG}{dt}$$